

## PROBLEM OF THE MONTH

DEPARTMENT OF MATHEMATICS  
ELMHURST UNIVERSITY  
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**Problem.** Frank Ilett, a dedicated Manchester United (MU) fan, promised not to get a haircut until his team wins five consecutive games. MU has recently improved and now has a 70% chance (probability = 0.7) of winning any individual game. We want to answer the following question: on average how many games will Frank need to watch before MU wins five games in a row and he can get his haircut?

- (1) Write some code to simulate this experiment and estimate the expected number of games.
  - (2) Use mathematical reasoning to verify the simulation's result.
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Scan the following QR code for submission instructions.

